

### Inversion-I.

It is required to solve 2 problems to pass the task.

**Problem 1.** Given a circle  $\omega$  with center  $O$  and arbitrary point  $A$  construct the image of point  $A$  under inversion with respect to  $\omega$  with *a)* ruler and compass; *b)* compass only.

**Problem 2.** Prove that for any two circles  $\omega_1$  and  $\omega_2$  there exists inversion taking them to *a)* equal circles; *b)* to concentric circles, if they do not intersect.

**Problem 3.** Given a point  $A$  and two circles  $\omega_1$  and  $\omega_2$  construct a circle  $\omega$  passing through  $A$  and tangent to  $\omega_1$  and  $\omega_2$ . How many solution does this problem have?

### Inversion-I.

It is required to solve 2 problems to pass the task.

**Problem 1.** Given a circle  $\omega$  with center  $O$  and arbitrary point  $A$  construct the image of point  $A$  under inversion with respect to  $\omega$  with *a)* ruler and compass; *b)* compass only.

**Problem 2.** Prove that for any two circles  $\omega_1$  and  $\omega_2$  there exists inversion taking them to *a)* equal circles; *b)* to concentric circles, if they do not intersect.

**Problem 3.** Given a point  $A$  and two circles  $\omega_1$  and  $\omega_2$  construct a circle  $\omega$  passing through  $A$  and tangent to  $\omega_1$  and  $\omega_2$ . How many solution does this problem have?